

Discrete Mathematics

Q1 Let $A = \{a, b, c, d, e, f, g, h\}$. Consider the following subsets of A

$$A_1 = \{a, b, c, d\} \quad A_2 = \{a, c, e, g, h\}$$

Determine whether $\{A_1, A_2\}$ is partition of set A or not.

- a) Yes
- b) No

Q2. Statement $(A \cap B)^c = A^c \cup B^c$ is known as

- a) Idempotent law
- b) Identity law
- c) De Morgan's law
- d) Distributive law

Q3. The power set $P(A)$ of $A = \{a, b, c, d\}$ contains the following no of elements:

- a) 4
- b) 8
- c) 16
- d) 32

Q4. Statement $(P \rightarrow Q) \vee (Q \rightarrow P)$ is

- a) Contradiction
- b) Tautology
- c) Absurdity
- d) None of above

Q5. Find the number of 3 letter words that can be formed from the word 'SERIES'

- a) 24
- b) 42
- c) 48
- d) 32

Q6 Let f be defined recursively by $f(n+1) = 2f(n) + 3$, $f(0) = 3$. Determine $f(1)$.

- a) 7
- b) 8
- c) 9
- d) 10

Q7 Let f be defined recursively by $f(n+1) = 2f(n) + 3$, $f(0) = 3$. Determine $f(2)$.

- a) 3
- b) 9
- c) 18
- d) 21

Q8. Let f be defined recursively by $f(n+1) = 2f(n) + 3$, $f(0) = 3$. Determine $f(3)$.

- a) 9
- b) 18
- c) 21
- d) 45

Q9. Let f be defined recursively by $f(n+1) = 2f(n) + 3$, $f(0) = 3$. Determine $f(4)$.

- a) 93
- b) 94
- c) 95
- d) 96

Q. 10. Consider the following collections of subsets of $S = \{1, 2, \dots, 8, 9\}$:

(i) $[\{1, 3, 5\}, \{2, 6\}, \{4, 8, 9\}]$

Identify if they are partitions of the given set or not.

- a) Yes
- b) No

Q. 15. Consider the following collections of subsets of $S = \{1, 2, \dots, 8, 9\}$:

(i) $[\{1, 3, 5\}, \{2, 4, 6, 8\}, \{5, 7, 9\}]$

Identify if they are partitions of the given set or not.

- a) Yes
- b) No

Q16. A partial ordered relation is Antisymmetric, reflexive and _____

- a) Transitive
- b) Symmetric
- c) Anti reflexive
- d) Asymmetric

Q16. The complete graph with four vertices has k edges where k is

- a) 3
- b) 4
- c) 5
- d) 6

Q17. Let $U = \{1, 2, 3, \dots, 9\}$ be the universal set, and let $A = \{1, 3, 4, 6\}$ and $B = \{5, 8, 9\}$ be the sets. The set $A \oplus B$ is

- a) $\{1, 2, 4, 5, 6, 8, 9\}$
- b) $\{1, 3, 4, 5, 6, 8, 9\}$
- c) $\{2, 3, 4, 5, 6, 8, 9\}$
- d) $\{1, 2, 3, 4, 5, 8, 9\}$

Q18. 34 farmers answered a questionnaire in which 18 said that they produce apples, 20

said they produce pears and 2 said that they produce neither. How many produce both apples and pears?

- a) 6
- b) 12
- c) 18
- d) 20

Q19. There is a drawer with sufficiently many red, blue, yellow and black socks inside of

it. How many socks we must pull in order to guarantee to have one pair?

- a) 9
- b) 5
- c) 15
- d) 18

Q20. Let the functions $f: N \rightarrow N$ and $g: Z \rightarrow N$ be defined as follows: $f(x) = 3x + 2$ and $g(x) = x^2 + 1$. Specify the functions $f \circ g$

- a) $5x^2 + 3$
- b) $3x^2 + 2$
- c) $2x^2 + 3$
- d) $3x^2 + 5$

Q21. Given the arithmetic sequence where $a_1 = 6$ and $a_5 = -6$. What is a_3 ?

- a) 0
- b) 1
- c) 2
- d) 3

Q22. Let $A = \{3,5,7,9\}$, $B = \{2,3,5,6,7\}$, and $C = \{2,4,6,8\}$ be all subjects of the universe $U = \{2,3,4,5,6,7,8,9\}$. Find $A \oplus B$

- a) $\{2,3,6\}$
- b) $\{3,6,9\}$
- c) $\{2,6,9\}$
- d) $\{2,6,8\}$

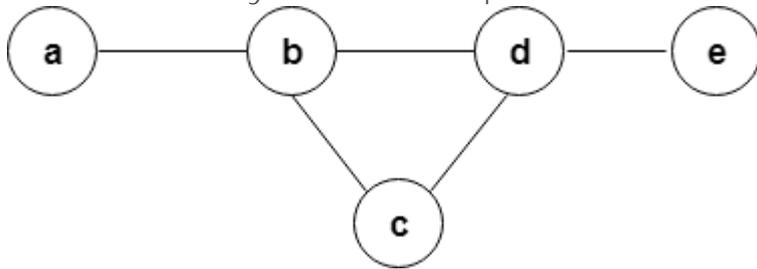
Q23. Let $A = \{3,5,7,9\}$, $B = \{2,3,5,6,7\}$, and $C = \{2,4,6,8\}$ be all subjects of the universe $U = \{2,3,4,5,6,7,8,9\}$. Find the compliment of C.

- a) $C^c = \{3,5,7,9\}$
- b) $C^c = \{2,5,7,9\}$
- c) $C^c = \{3,5,6,9\}$
- d) $C^c = \{3,5,7,8\}$

Q24. In graphs, in which all vertices have an odd degree, the number of Hamiltonian cycles through any fixed edge is always even

- a) True
- b) False

Q25. How many Hamiltonian paths does the following graph have?



- a) 1
- b) 2
- c) 3
- d) 4